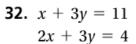
# WarmUp

Solve each system using elimination.



**33.** 
$$2x + 4y = -12$$
  
 $-6x + 5y = 2$ 

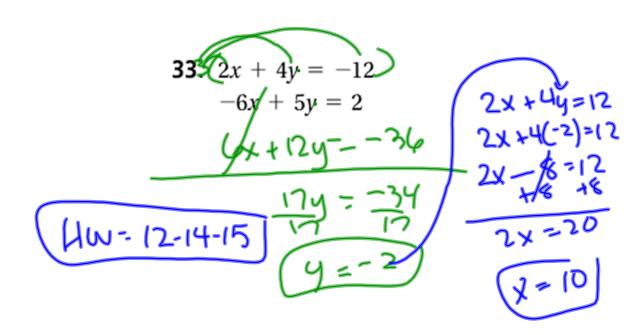
Solve each inequality. Check your solution.

**35.** 
$$3a + 5 > 20$$

**37.** 
$$3(q+4) \leq -2q-8$$







32. 
$$x + 3y = 11$$

$$-1(2x + 3y = 4)$$

$$-2 + -3y = -4$$

$$-1 + 3y = 11$$

$$-1(-x) = 11$$

$$-(7) = 1$$

$$-(7) = 1$$



#### **©** Content Standards

**A.REI.6** Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs of linear equations in two variables.

Also N.Q.2, N.Q.3, A.CED.3

**Objective** To choose the best method for solving a system of linear equations

### ake note

### Concept Summary Choosing a Method for Solving Linear Systems

Method When to Use

Graphing When you want a visual display of the equations, or when you want to estimate a solution

Substitution When one equation is already solved for one of the variables, or when

it is easy to solve for one of the variables

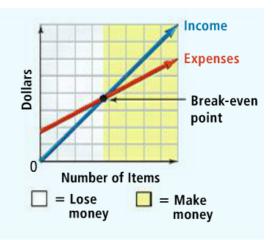
**Elimination** When the coefficients of one variable are the same or opposites, or

when it is not convenient to use graphing or substitution

Systems of equations are useful for modeling problems involving mixtures, rates, and break-even points.

The break-even point for a business is the point at which income equals expenses. The graph shows the break-even point for one business.

Notice that the values of *y* on the red line represent dollars spent on expenses. The values of *y* on the blue line represent dollars received as income. So *y* is used to represent both expenses and income.



## Problem 1 Finding a Break-Even Point

**Business** A fashion designer makes and sells hats. The material for each hat costs \$5.50. The hats sell for \$12.50 each. The designer spends \$1400 on advertising. How many hats must the designer sell to break even?

Step 1 Write a system of equations. Let x = the number of hats sold, and let y = the number of dollars of expense or income.

Expense: y = 5.5x + 1400 Income: y = 12.5x

**Step 2** Choose a method. Use substitution since both equations are solved for *y*.

y = 5.5x + 1400 Start with one equation. 12.5x = 5.5x + 1400 Substitute 12.5x for y.

2.3x 3.3x 1 1400 Substitute 12.3x 101 y.

7x = 1400 Subtract 5.5x from each side. x = 200 Divide each side by 7.

Since *x* is the number of hats, the designer must sell 200 hats to break even.



Got lt? 1. A puzzle expert wrote a new sudoku puzzle book. His initial costs are \$864. Binding and packaging each book costs \$.80. The price of the book is \$2. How many copies must be sold to break even?

In real-world situations, you need to consider the constraints described in the problem in order to write equations. Once you solve an equation, you need to consider the viability of the solution. For example, a solution that has a negative number of hours is not a viable solution.

# Problem 2 Identifying Constraints and Viable Solutions

**Zoo** The local zoo is filling two water tanks for the elephant exhibit. One water tank contains 50 gal of water and is filled at a constant rate of 10 gal/h. The second water tank contains 29 gal of water and is filled at a constant rate of 3 gal/h. When will the two tanks have the same amount of water? Explain.

**Step 1** Write a system of equations. Let x = the number of hours the tanks are filling and let y = the number of gallons in the tank.

Tank 1: 
$$y = 10x + 50$$
 Tank 2:  $y = 3x + 29$ 

**Step 2** The system is easy to solve using substitution. Substitute 10x + 50 for y in the second equation and solve for x.

$$y=3x+29$$
 Write the second equation.  
 $10x+50=3x+29$  Substitute  $10x+50$  for  $y$ .  
 $7x+50=29$  Subtract  $3x$  from each side. Then simplify.  
 $7x=-21$  Subtract  $50$  from each side. Then simplify.  
 $x=-3$  Divide each side by  $7$ .

**Step 3** Substitute -3 for x in either equation and solve for y.

$$y = 10(-3) + 50$$
 Substitute  $-3$  for  $x$  in the first equation.  
 $y = 20$  Simplify.

The solution to the system is (-3, 20). The solution (-3, 20) is not a viable solution because it is not possible to have time be -3 hours. So, the tanks never have the same amount of water.



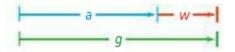
Got It? 2. The zoo has two other water tanks that are leaking. One tank contains  $10\ \mathrm{gal}$  of water and is leaking at a constant rate of 2 gal/h. The second tank contains 6 gal of water and is leaking at a constant rate of 4 gal/h. When will the tanks have the same amount of water? Explain.

When a plane travels from west to east across the United States, the steady west-to-east winds act as tailwinds. This increases the plane's speed relative to the ground. When a plane travels from east to west, the winds act as headwinds. This decreases the plane's speed relative to the ground.

#### From West to East

#### From East to West

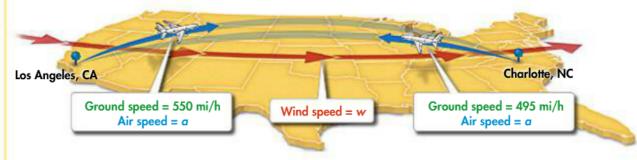
air speed + wind speed = ground speed = air speed - wind speed = ground speed





## Problem 3 Solving a Wind or Current Problem

**Travel** A traveler flies from Charlotte, North Carolina, to Los Angeles, California. At the same time, another traveler flies from Los Angeles to Charlotte. The air speed of each plane is the same. The ground speeds are shown below. What is the air speed? What is the wind speed?



Use the ground speed with the tailwind and with the headwind to write the system. Let a = the air speed of the planes. Let w = the wind speed.

$$\frac{\text{air}}{\text{speed}} + \frac{\text{wind}}{\text{speed}} = \frac{\text{ground speed}}{\text{with tailwind}} + \frac{\text{air}}{\text{speed}} - \frac{\text{wind}}{\text{speed}} = \frac{\text{ground speed}}{\text{with headwind}}$$
 $\frac{a}{a} + \frac{w}{w} = 550$ 
 $\frac{a}{a} - \frac{w}{w} = 495$ 

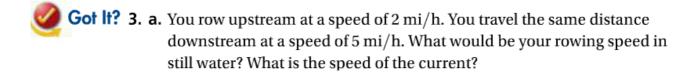
Choose a method to solve the system. Use elimination.

$$a+w=550$$
 $a-w=495$ 
 $2a+0=1045$  Add the equations.
 $a=522.5$  Solve for  $a$ .

Substitute 522.5 for a in either equation and solve for w.

$$522.5 + w = 550$$
 Substitute 522.5 for a in the first equation.  $w = 27.5$  Solve for w.

The air speed is 522.5 mi/h. The wind speed is 27.5 mi/h.



### CW - Page 390 (6-4)

- **7. Business** A bicycle store costs \$2400 per month to operate. The store pays an average of \$60 per bike. The average selling price of each bicycle is \$120. How many bicycles must the store sell each month to break even?
- **8. Theater** Producing a musical costs \$88,000 plus \$5900 per performance. One sold-out performance earns \$7500 in revenue. If every performance sells out, how many performances are needed to break even?
- **9. Investment** You split \$1500 between two savings accounts. Account A pays annual 5% interest and Account B pays 4% annual interest. After one year, you have earned a total of \$69.50 in interest. How much money did you invest in each account? Explain.
- **10. Biology** A group of scientists studied the effect of a chemical on various strains of bacteria. Strain A started with 6000 cells and decreased at a constant rate of 2000 cells per hour after the chemical was applied. Strain B started with 2000 cells and decreased at a constant rate of 1000 cells per hour after the chemical was applied. When will the strains have the same number of cells? Explain.
- **11. Airports** A traveler is walking on a moving walkway in an airport. The traveler must walk back on the walkway to get a bag he forgot. The traveler's groundspeed is 2 ft/s against the walkway and 6 ft/s with the walkway. What is the traveler's speed off the walkway? What is the speed of the moving walkway?
- 12. Kayaking A kayaker paddles upstream from camp to photograph a waterfall and returns. The kayaker's speed while traveling upstream and downstream is shown below. What is the kayaker's speed in still water? What is the speed of the current?



- **13.** Money You have a jar of pennies and quarters. You want to choose 15 coins that are worth exactly \$4.35.
  - **a.** Write and solve a system of equations that models the situation.
  - b. Is your solution reasonable in terms of the original problem? Explain.

Solve each system. Explain why you chose the method you used.

**14.** 
$$4x + 5y = 3$$

$$3x - 2y = 8$$

**15.** 
$$2x + 7y = -20$$

$$y = 3x + 7$$

**16.** 
$$5x + 2y = 17$$

$$x - 2y = 8$$



 $\bigcirc$  17. Reasoning Find A and B so that the system below has the solution (2,3).

$$Ax - 2By = 6$$
$$3Ax - By = -12$$



- 18. Think About a Plan A tugboat can pull a boat 24 mi downstream in 2 h. Going upstream, the tugboat can pull the same boat 16 mi in 2 h. What is the speed of the tugboat in still water? What is the speed of the current?
  - How can you use the formula d = rt to help you solve the problem?
  - How are the tugboat's speeds when traveling upstream and downstream related to its speed in still water and the speed of the current?
- Open-Ended Without solving, decide which method you would use to solve each system: graphing, substitution, or elimination. Explain.

**19.** 
$$y = 3x - 1$$
  $y = 4x$ 

**20.** 
$$3m - 4n = 1$$
  $3m - 2n = -1$ 

**21.** 
$$4s - 3t = 8$$
  $t = -2s - 1$ 

- **22.** Business A perfume maker has stocks of two perfumes on hand. Perfume A sells for \$15 per ounce. Perfume B sells for \$35 per ounce. How much of each should be combined to make a 3-oz bottle of perfume that can be sold for \$63?
- **1EM 23. Chemistry** In a chemistry lab, you have two vinegars. One is 5% acetic acid, and one is 6.5% acetic acid. You want to make 200 mL of a vinegar with 6% acetic acid. How many milliliters of each vinegar do you need to mix together?
  - **24.** Boating A boat is traveling in a river with a current that has a speed of 1.5 km/h. In one hour, the boat can travel twice the distance downstream that it can travel upstream. What is the boat's speed in still water?
- - 25. Reasoning A student claims that the best way to solve the system at the right is by substitution. Do you agree? Explain.

**26. Entertainment** A contestant on a quiz show gets 150 points for every correct answer and loses 250 points for each incorrect answer. After answering 20 questions, the contestant has 200 points. How many questions has the contestant answered correctly? Incorrectly?